

## Cambridge O Level

# ADDITIONAL MATHEMATICS Paper 2 MARK SCHEME Maximum Mark: 80 Published

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

Cambridge International will not enter into discussions about these mark schemes.

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This document consists of 10 printed pages.

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## **Generic Marking Principles**

These general marking principles must be applied by all examiners when marking candidate answers. They should be applied alongside the specific content of the mark scheme or generic level descriptors for a question. Each question paper and mark scheme will also comply with these marking principles.

### GENERIC MARKING PRINCIPLE 1:

Marks must be awarded in line with:

- the specific content of the mark scheme or the generic level descriptors for the question
- the specific skills defined in the mark scheme or in the generic level descriptors for the question
- the standard of response required by a candidate as exemplified by the standardisation scripts.

### **GENERIC MARKING PRINCIPLE 2:**

Marks awarded are always **whole marks** (not half marks, or other fractions).

### **GENERIC MARKING PRINCIPLE 3:**

Marks must be awarded **positively**:

- marks are awarded for correct/valid answers, as defined in the mark scheme. However, credit is given for valid answers which go beyond the scope of the syllabus and mark scheme, referring to your Team Leader as appropriate
- marks are awarded when candidates clearly demonstrate what they know and can do
- marks are not deducted for errors
- marks are not deducted for omissions
- answers should only be judged on the quality of spelling, punctuation and grammar when these features are specifically assessed by the question as indicated by the mark scheme. The meaning, however, should be unambiguous.

### GENERIC MARKING PRINCIPLE 4:

Rules must be applied consistently, e.g. in situations where candidates have not followed instructions or in the application of generic level descriptors.

## GENERIC MARKING PRINCIPLE 5:

Marks should be awarded using the full range of marks defined in the mark scheme for the question (however; the use of the full mark range may be limited according to the quality of the candidate responses seen).

## GENERIC MARKING PRINCIPLE 6:

Marks awarded are based solely on the requirements as defined in the mark scheme. Marks should not be awarded with grade thresholds or grade descriptors in mind.

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Ma	Maths-Specific Marking Principles				
1	Unless a particular method has been specified in the question, full marks may be awarded for any correct method. However, if a calculation is required then no marks will be awarded for a scale drawing.				
2	Unless specified in the question, answers may be given as fractions, decimals or in standard form. Ignore superfluous zeros, provided that the degree of accuracy is not affected.				
3	Allow alternative conventions for notation if used consistently throughout the paper, e.g. commas being used as decimal points.				
4	Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored (isw).				
5	Where a candidate has misread a number in the question and used that value consistently throughout, provided that number does not alter the difficulty or the method required, award all marks earned and deduct just 1 mark for the misread.				
6	Recovery within working is allowed, e.g. a notation error in the working where the following line of working makes the candidate's intent clear.				

## MARK SCHEME NOTES

The following notes are intended to aid interpretation of mark schemes in general, but individual mark schemes may include marks awarded for specific reasons outside the scope of these notes.

## Types of mark

- M Method marks, awarded for a valid method applied to the problem.
- A Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. For accuracy marks to be given, the associated Method mark must be earned or implied.
- B Mark for a correct result or statement independent of Method marks.

When a part of a question has two or more 'method' steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. The notation 'dep' is used to indicate that a particular M or B mark is dependent on an earlier mark in the scheme.

## **Abbreviations**

awrt answers which round to
cao correct answer only
dep dependent
FT follow through after error

isw ignore subsequent working
nfww not from wrong working

oe or equivalent

rot rounded or truncated

SC Special Case soi seen or implied

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Question	Answer	Marks	Guidance
1	$2x^2 - 8x + 3x - 12 \cdot 3x^2 - 3x + 4x - 4$	B1	Correctly expands all brackets * is any inequality or equals sign
	$[0*] x^2 + 6x + 8$	B1	Collects terms to correct 3-term quadratic in solvable form
	[0*](x+2)(x+4)	M1	Factorises or solves <i>their</i> 3-term quadratic
	−4 and −2	A1	Correct critical values
	$-4 \le x \le -2$ mark final answer	A1	
2	$\frac{\mathrm{d}y}{\mathrm{d}x} = 2ax - 5$	B1	
	$2a \times 2 - 5 = 7  \text{oe}$	M1	$\mathbf{FT} \ their \left( \frac{\mathrm{d}y}{\mathrm{d}x} \Big _{x=2} \right) = 7$
	a=3	A1	
	$7 \times 2 + b = their 4$ or $b = 2 - 4 \times their a$	M1	<b>dep</b> on previous M1 where <i>their</i> 4 is an attempt to evaluate $y = ax^2 - 5x + 2$ using $x = 2$ and <i>their a</i>
	b = -10	A1	
	Alternative		
	$(-12)^2 - 4a(2-b) = 0$ oe	(B1)	for use of discriminant on $ax^2 - 12x + 2 - b = 0$
	144 - 8a + 4a(4a - 22) = 0  oe or $144 - (b + 22)(2 - b) = 0  oe$	(M1)	Condone one sign or arithmetic error
	$a^2 - 6a + 9 = 0$ oe or $b^2 + 20b + 100 = 0$ oe	(A1)	for correct 3-term quadratic in solvable form
	a=3 and $b=-10$	(A2)	<b>A1</b> for $a = 3$ or $b = -10$

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Question	Answer	Marks	Guidance
3	$\lg((2x-1)(x+2)) = \lg \frac{100}{4} \text{ oe}$ or $10^2 = 4(2x-1)(x+2)$ oe	M2	M1 for one log law correctly applied within a correct equation e.g. $lg4(2x-1)(x+2) = 2$
	$2x^2 + 3x - 27[=0]$	A1	Collects terms to correct 3-term quadratic in solvable form
	(2x+9)(x-3)[=0]	M1	<b>dep</b> on at least <b>M1</b> previously awarded Factorises their $2x^2 + 3x - 27$ or solves their $2x^2 + 3x - 27 = 0$
	x = 3 indicated as only valid solution	A1	nfww
4(a)	2k+6=8-16+6k+2 oe	M1	For equating line to curve and substituting $x = 2$ , or vice versa
	k=3	A1	
4(b)	$x^{3}-4x^{2}+(2\times their k)x-4 = 0$ or $x^{3}-4x^{2}+6x-4 = 0$	M1	FT their k in correct cubic
	$x^2 - 2x + 2$	A2	Correct quadratic factor from correct cubic  A1 for a quadratic factor with two terms correct, from correct cubic
	$(-2)^2 - 4(1)(2) < 0$ oe or $4 - 8 < 0$ oe	A1	Uses discriminant correctly on the correct quadratic factor
	[and so $x = 2$ is the only solution]		

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Question	Answer	Marks	Guidance
5(a)	$\frac{\cos^2 x + (1-\sin x)^2}{(1-\sin x)\cos x}$	M1	Correctly takes common denominator
	or $\frac{\cos^2 x}{(1-\sin x)\cos x} + \frac{(1-\sin x)^2}{(1-\sin x)\cos x}$		
	$\frac{\cos^2 x + 1 - 2\sin x + \sin^2 x}{\left(1 - \sin x\right)\cos x}$	A1	OR $\frac{1-\sin^2 x + (1-\sin x)^2}{\left(1-\sin x\right)\cos x}$
	$\frac{1+1-2\sin x}{(1-\sin x)\cos x}$ or $\frac{1-\sin^2 x+1-2\sin x+\sin^2 x}{(1-\sin x)\cos x}$	A1	OR $\frac{(1-\sin x)(1+\sin x)+(1-\sin x)^2}{(1-\sin x)\cos x}$
	$\frac{2(1-\sin x)}{(1-\sin x)\cos x} = 2\sec x$ or $\frac{2-2\sin x}{(1-\sin x)\cos x} = \frac{2}{\cos x} = 2\sec x$	A1	All steps correct and final step justified  OR $\frac{1+\sin x + 1 - \sin x}{\cos x} = 2\sec x$
	or equivalent		
	Alternative Must work with LHS only		
	$\frac{(\cos x)(1+\sin x)}{(1-\sin x)(1+\sin x)} + \frac{(1-\sin x)\cos x}{(\cos x)\cos x}$	(M1)	Forms fractions with common denominator in different form
	$\frac{(\cos x)(1+\sin x)}{\cos^2 x} + \frac{(1-\sin x)\cos x}{\cos^2 x}$	(A1)	Uses difference of two squares and $\sin^2 x + \cos^2 x = 1$ to write fractions with a common denominator in the same form
	$\frac{2\cos x}{\cos^2 x}$	(A1)	Combine as a single fraction and collects terms
	$\frac{2}{\cos x} = 2\sec x$	(A1)	All steps correct and final step justified
5(b)	$\cos^3\frac{\theta}{2} = \frac{1}{4}$	B1	
	$\cos\frac{\theta}{2} = \sqrt[3]{their \frac{1}{4}} \text{ soi}$	M1	<b>dep</b> on starting with $2\sec\frac{\theta}{2} = 8\cos^2\frac{\theta}{2}$
	±101.9 awrt	A2	and no extras in range  A1 for either, ignoring extras in range  If A0 then SC1 for ±102 with no  extras in range

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Question	Answer	Marks	Guidance
6	$81+108ax+54a^{2}x^{2}+12a^{3}x^{3} \text{ soi}$ or $12a^{3} = \frac{3}{2} b=108a c=54a^{2} \text{ soi}$	M3	M2 for any 3 correct terms or 2 correct equations or M1 for any 2 correct terms, 1 correct equation or for correct but insufficiently simplified expansion e.g. $3^4 + 4 \times 3^3 \times ax + \frac{4 \times 3}{2} \times 3^2 \times (ax)^2 + \frac{4 \times 3 \times 2}{3 \times 2} \times 3 \times (ax)^3$
	$a = \frac{1}{2}$ oe	A1	
	<i>b</i> = 54	A1	FT 108 × their a, providing at least M1 awarded
	$c = \frac{27}{2} \text{ oe}$	A1	FT $54 \times (their\ a)^2$ , providing at least M1 awarded
7	${}^{n}C_{4} = \frac{n!}{(n-4)!4!}$ and ${}^{n}C_{2} = \frac{n!}{(n-2)!2!}$ soi	В1	
	$\frac{n(n-1)(n-2)(n-3)}{24} = \frac{13n(n-1)}{2}$ or $(n-2)(n-3) = \frac{13 \times 24}{2}$ oe, soi	M1	Writes in a correct form, free of factorials
	$n^2 - 5n - 150$ [=0]	<b>A1</b>	
	n = 15 only, nfww	<b>A1</b>	dep on previous A1
	$^{15}C_8 = 6435$ only	B1	
8(a)	(Velocity vector =) $\frac{26}{\sqrt{12^2 + 5^2}} \binom{12}{5}$ oe	M2	<b>M1</b> for $\sqrt{12^2 + 5^2}$ or 13 or 2 seen
	(Position vector =) $\begin{pmatrix} 3 \\ -2 \end{pmatrix} + t \begin{pmatrix} 24 \\ 10 \end{pmatrix}$ oe	A1	

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Question	Answer	Marks	Guidance
8(b)	(Direction vector =) $\begin{pmatrix} 4 \\ 3 \end{pmatrix}$ soi or $x$ component: $\cos \alpha = \frac{4}{5}$	B1	
	y component: $\sin \alpha = \frac{3}{5}$ soi		
	(Velocity vector =) $\frac{20}{\sqrt{4^2 + 3^2}} \times their \begin{pmatrix} 4 \\ 3 \end{pmatrix}$ oe soi $(their\cos\alpha)$	M1	
	or $20 \begin{pmatrix} their\cos\alpha \\ their\sin\alpha \end{pmatrix}$ soi		
	(Position vector =) $\begin{pmatrix} 67 \\ -18 \end{pmatrix} + t \begin{pmatrix} 16 \\ 12 \end{pmatrix}$ oe	A2	<b>A1 FT</b> $\begin{pmatrix} 67 \\ -18 \end{pmatrix} + t \times their \begin{pmatrix} 16 \\ 12 \end{pmatrix}$
			If zero scored, <b>SC2</b> for one correct component, either 67+16 <i>t</i> or -18+12 <i>t</i>
8(c)	3+24t = 67+16t oe or $-2+10t = -18+12t$ oe	M1	<b>FT</b> Equates <i>their</i> $x$ components, or <i>their</i> $y$ components from parts (a) and (b), providing of equivalent difficulty, e.g. $a+bt=c+dt$
	t = 8	<b>A1</b>	dep on full marks in (a) and (b)
	(Position of meeting =) $\binom{195}{78}$	<b>A1</b>	dep on full marks in (a) and (b)
9(a)	$\frac{\mathrm{d}}{\mathrm{d}x} \left( \mathrm{e}^{-2x} \right) = -2\mathrm{e}^{-2x} \text{ soi}$	B1	
	$\frac{\mathrm{d}y}{\mathrm{d}x} = k\mathrm{e}^{-2x} - 2kx\mathrm{e}^{-2x} \text{ oe, isw}$	B1	FT for use of product rule $k.e^{-2x} + kx. \left(their \frac{d}{dx} \left(e^{-2x}\right)\right)$
	Alternative		
	$\frac{\mathrm{d}}{\mathrm{d}x} \left( \mathrm{e}^{2x} \right) = 2\mathrm{e}^{2x} \text{ soi}$	(B1)	
	$\frac{dy}{dx} = \frac{ke^{2x} - 2kxe^{2x}}{\left(e^{2x}\right)^2} \text{ oe, isw}$	(B1)	FT for use of quotient rule $\frac{k \cdot e^{2x} - kx \cdot \left(their  2e^{2x}\right)}{\left(e^{2x}\right)^2}$

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Question	Answer	Marks	Guidance
9(b)	Equates $\frac{dy}{dx} = 0$ and finds $10 - 20x = 0$ oe	M1	FT their (a), provided of the form $me^{-2x} + nxe^{-2x} \text{ or } me^{2x} + nxe^{2x}$
	$\left(\frac{1}{2}, \frac{5}{e}\right)$ oe only	A2	For both values: $x = 0.5$ <b>and</b> $y = 5e^{-1}$ or 1.84 or 1.839[39] rot to 4 or more sf <b>A1</b> for $x = \frac{1}{2}$ only
9(c)	$-2xe^{-2x} - e^{-2x} + c$	В3	For fully correct answer or <b>B2</b> for $-2xe^{-2x} - e^{-2x}$ or $\left[ \int 4xe^{-2x} dx \right] = -2xe^{-2x} + \int 2e^{-2x} dx$ or <b>B1</b> for $kxe^{-2x} = \int \left( ke^{-2x} - 2kxe^{-2x} \right) dx$ or better
9(d)	$-2e^{-2} - e^{-2} - (0 - e^{0})$ oe	M1	Correct substitution of limits into correct expression
	$1 - \frac{3}{e^2}$ or $1 - 3e^{-2}$	<b>A1</b>	
10(a)	a + (3-1)d = 10 soi	B1	
	$\frac{8}{2} \{2a + (8-1)d\} = 116 \text{ soi}$	B1	
	Correct method to eliminate one unknown and attempt to solve to find <i>a</i> or <i>d</i>	M1	dep on at least B1 awarded
	a = 4 and $d = 3$	<b>A2</b>	A1 for either
10(b)	$S_{30} = \frac{30}{2} \{ 2(4) + 29(3) \}$ and $S_{11} = \frac{11}{2} \{ 2(4) + 10(3) \}$	В2	<b>M1 FT</b> their a and their d for $S_{30} = \frac{30}{2} \{ 2(their 4) + 29(their 3) \}$ or $S_{11} = \frac{11}{2} \{ 2(their 4) + 10(their 3) \}$
	Correct plan $S_{30} - S_{11}$ attempted	M1	FT their a and their d
	1216	<b>A1</b>	

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Question	Answer	Marks	Guidance
10(b)	Alternative 1		
	first term = $4 + 11 \times 3$ or 37 and an attempt at $S_{19}$	(M1)	<b>FT</b> their $a + 11 \times their d$
	$\frac{19}{2} \{2(37) + (19-1) \times 3\} \text{ oe}$ or $\frac{19}{2} \{37 + 91\}$ oe	(B2)	M1 FT for their first term and their d in $\frac{19}{2}$ {2(their 37)+(19-1)×their 3} or for their first term and their last term in $\frac{19}{2}$ {their 37 + their 91}
	1216	(A1)	
	Alternative 2		
	Correct sum of terms: 37 + 40 + 43 + 46 + 49 + 52 + 55 + 58 + 61 + 64 + 67 + 70 + 73 + 76 + 79 + 82 + 85 + 88 + 91	(M3)	M2 FT their a and their d for sum starting with their 37 and ending with their 91, with at most one omission or error or M1 FT their a and their d for sum starting with their 37 or ending with their 91, with at most two omissions or errors
	1216	(A1)	
11(a)	$2\mathbf{a} + \lambda (3\mathbf{b} - 2\mathbf{a})$ oe isw or $3\mathbf{b} - (1 - \lambda)(3\mathbf{b} - 2\mathbf{a})$ oe isw	В3	<b>B1</b> for $\overrightarrow{PS} = 3\mathbf{b} - 2\mathbf{a}$ soi and <b>B1</b> for correct route using $\lambda$ , either $\overrightarrow{OX} = \overrightarrow{OP} + \lambda \overrightarrow{PS}$ soi or $\overrightarrow{OX} = \overrightarrow{OS} - (1 - \lambda) \overrightarrow{PS}$ soi
11(b)	$\mu(5\mathbf{a}+2\mathbf{b})$ isw	B2	<b>B1</b> for $\overrightarrow{OQ} = 3\mathbf{b} + 5\mathbf{a} - \mathbf{b}$ oe soi
11(c)	$2-2\lambda=5\mu$ and $3\lambda=2\mu$ oe	M2	for correctly equating scalars for both components  FT their (a) and (b) if possible  M1 FT for equating scalars for either component
	Solves to find $\lambda = \frac{4}{19}$ or $\mu = \frac{6}{19}$	<b>A1</b>	
	$\lambda = \frac{4}{19}$ and $\mu = \frac{6}{19}$	A1	
11(d)	$\frac{6}{19}$ isw	B1	
11(e)	$\frac{4}{15}$ isw	B1	

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